

An Electric Dipole in an Electric field

An Electric Dipole consists of two equal and opposite charges $+q$ and $-q$ separated by a very small distance a . Although in electric dipole, the two charges are equal and opposite so as to give a zero net charge. yet they are displaced slightly. It produces a non-vanishing space field.

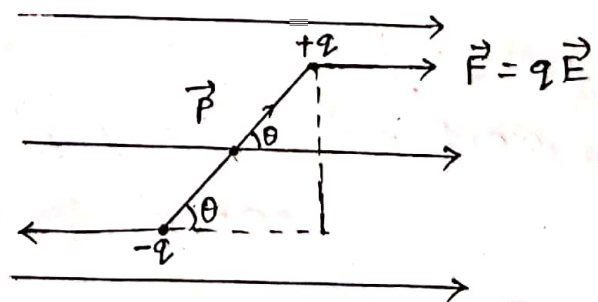
The electric dipole moment \vec{p} is defined as $\vec{p} = q\vec{a}$

where \vec{a} is displacement from the negative to positive charge.

The electric dipole moment \vec{p} directs along the axis of the dipole pointing from negative to positive charge.

Let an electric dipole is placed in a uniform external electric field \vec{E} , making an angle θ

with the field. The charge $+q$ experiences a force $q\vec{E}$ in the direction of the field. while the charge $-q$ experiences an equal force in the opposite direction. These



two equal and opposite forces parallel to each other form a ~~clockwise~~ clockwise couple. It tends to set the dipole in the direction of the electric field. The torque τ of the couple is given by

$$\tau = qE(a \sin \theta)$$

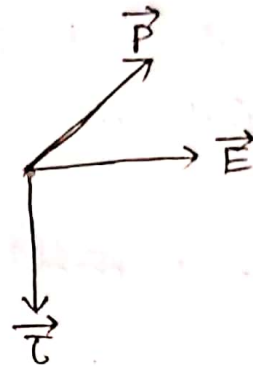
$$\tau = qa(E \sin \theta)$$

$$\tau = pE \sin \theta \quad (\because p = qa)$$

In vector form, the above expression may be written as

$$\vec{\tau} = \vec{p} \times \vec{E}$$

In this figure shows the direction of the vector. Thus an electric dipole released in an electric field experiences a couple which tends to align the dipole parallel to the field.



When the dipole moment p is parallel to the field \vec{E} , it is in stable equilibrium. It is so because as soon as it is displaced through an angle θ , torque $pE \sin \theta$ brings it back parallel to the field.

When \vec{p} and \vec{E} are in opposite direction ($\theta = 180^\circ$), ~~the~~ the torque on it is zero and the dipole is equilibrium. But the equilibrium is unstable because any displacement from this position gives a torque which sets it along the field.